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## THE KENYA NATIONAL EXAMINATIONS COUNCIL Kenya Certificate of Secondary Education

121/2 Compressor Free Version

# **MATHEMATICS** ALT A

Mar. 2022 - 21/2 hours



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# SECTION I (50 marks)

## **PDF Compressor Free Version**

Answer all the questions in this section in the spaces provided.

An empty tank of capacity 18480 litres is to be filled with water using a cylindrical pipe of 1. diameter 0.028 m. The rate of flow of water from the pipe is 2 m/s. Find the time in hours it would take to fill up the tank. (Take  $\pi = \frac{22}{7}$ ).

The first term of a Geometric Progression (G.P) is 2. The common ratio of the G.P is also 2. The product of the last two terms of the G.P is 512. Determine the number of terms in the G.P. 2. (3 marks)

Last term = 
$$2(2^{n-1})$$
  
 $2^{n-3} = 128 = 2^7$   
Last term =  $2(2^{n-1})$   
 $2^{n-3} = 128 = 2^7$   
 $2^{n-3} = 7$   
 $2^{n-3} = 7$ 

3. (2 marts)

Aff. 1  
Using diseriminant:  

$$b^2 = 4ac$$
  
 $(30)^2 = 4(9)(9)$   
 $\Rightarrow 0 = 25$ 

Let 
$$ax^{2}-36x+9=(kx-b)^{2}$$
 $ax^{2}-36x+9=(kx-b)^{2}$ 
 $ax^{2}-30x+9=k^{2}x^{2}-3kbx+b^{2}$ 
Comparing,
 $q=b^{2}\Rightarrow b=\pm 3$ 
And  $30=2kb\Rightarrow k=\pm 5$ 
And  $q=k^{2}\Rightarrow q=25$ 

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Youring both sides,

$$y^2 = \frac{b^2x^2}{cx^2 - q}$$

$$\Rightarrow y^2(cx^2 - b^2) = ay^2$$

$$\Rightarrow x^2(cy^2 - b^2) = ay^2$$

$$\Rightarrow x^2 = \frac{ay^2}{cy^2 - b}$$

$$\Rightarrow y^{2}Cx^{2} - b^{2}x^{2} = ay^{2}$$

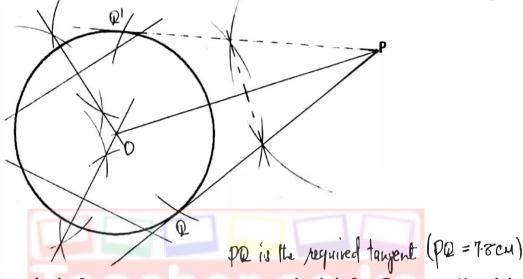
$$\Rightarrow x^{2}(cy^{2} - b^{2}) = ay^{2}$$

$$x^{2} = \frac{ay^{2}}{cy^{2} - b^{2}}$$

$$\Rightarrow x = +\sqrt{\frac{ay^{2}}{cy^{2} - b^{2}}}$$

$$\Rightarrow circle$$

5. The figure below shows a circle and a point P outside the circle



Using a ruler and pair of compasses, construct a tangent to the circle from P.

(4 marks)

6. Four quantities P, Q, R and S are such that P varies directly as the square root of Q and inversely as the square of the difference of R and S. Quantity Q is increased by 44% while quantities R and S are each decreased by 10%.

Find the corresponding percentage change in P correct to 1 decimal place.

(4 marks)

$$P\alpha \frac{\sqrt{Q}}{(R-S)^{2}} \Rightarrow P = \frac{\kappa \sqrt{Q}}{(R-S)^{2}}$$

$$P' = \frac{\kappa \sqrt{1.44Q}}{[0.q(R-S)]^{2}}$$

$$= \frac{1.2}{0.q^{2}} \frac{\kappa \sqrt{Q}}{(R-S)^{2}}$$

$$\Rightarrow P' = \frac{40}{27}P$$

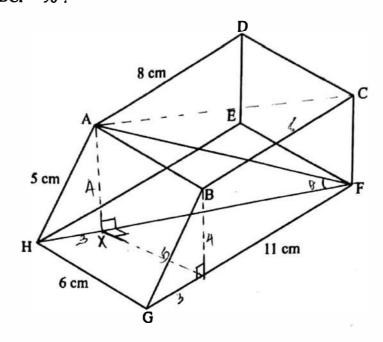
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7. The figure below represents a prism ABCDEFGH of length 6 cm. The cross section BCFG of PDF Chappisms artrapes ungh which GF = 11 cm, BC = 8 cm, BG = 5 cm and  $\angle$  GFC =  $\angle$  BCF = 90°.



Calculate correct to 1 decimal place the angle between the line FA and the plane GFEH.

FH = 
$$\sqrt{6^2 + 11^3} = \sqrt{157}$$
 tan  $o = \frac{4}{\sqrt{157} - 3}$ 

O = 22.8°

(or  $O = 21.8^\circ$  if  $FX = AC = 10$  cm is used)

8. The cash price of a gas cooker is Ksh 20 000. A customer bought the cooker on hire purchase terms by paying a deposit of Ksh 10 000 followed by 18 equal monthly instalments of Ksh 900 each. Annual interest, compounded quarterly, was charged on the balance for the period of 18 months. Determine, correct to 1 decimal place, the rate of interest per annum. (4 marks)

$$\dot{A} = P(1 + \frac{1}{100})^{1}$$

$$(18x 900) = (20000 - 10000)(1 + \frac{1}{400})^{1}$$

$$6 \overline{16200} = (1 + \frac{1}{400})$$

$$\dot{Y} = (6 \overline{1.62} - 1) \times 400$$

$$\dot{Y} = 33.56 \text{ New ya Certificate of Secondary Education, 2021}$$

$$13022 = 33.56 \text{ New ya Certificate of Secondary Education, 2021}$$



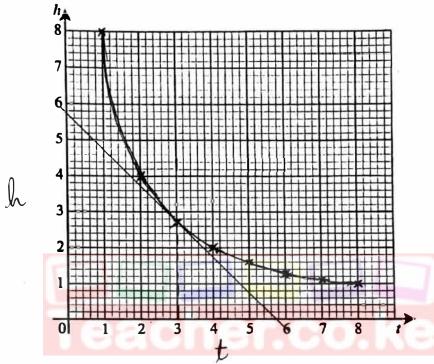
9. The table below shows the values of t and the corresponding values of t for a given relation.

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X	t	1	2	3	4	5	6	7	8
7	h	8	4	2.7	2	1.6	1.3	1.1	1

(a) On the grid provided, draw a graph to represent the information on the table given.

(2 marks)



(b) Use the graph to determine, correct to 1 decimal place, the rate of change of h at t = 3. (2 marks)

Note of change = gradient at 
$$t = 3$$

$$= \frac{47}{4x}$$

$$= 0-5.7$$

$$= -1.0$$



- 10. The equation of a trigonometric wave is  $y = 4 \sin (ax - 70)^{\circ}$ . The wave has a period of 180°.
  - **PDF Compressor Free Version** (a) Determine the value of a.

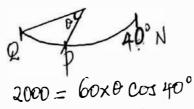
(1 mark)

$$\frac{360}{9} = 180^{\circ} \implies 9 = 2$$

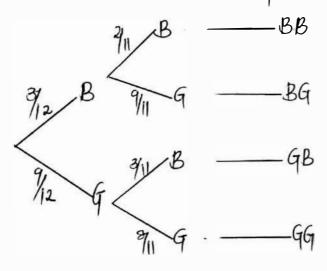
(b) Deduce the phase angle of the wave.

(1 mark)

A point Q is 2000 nm to the West of a point P(40°N, 155°W). Find the longitude of Q to the 11. (3 marks) nearest degree.



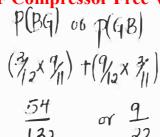
- 12. A box contains 3 brown balls and 9 green balls. The balls are identical except for the colours. Two balls are picked at random without replacement.
  - Draw a tree diagram to show all the possible outcomes. (1 mark) (a)



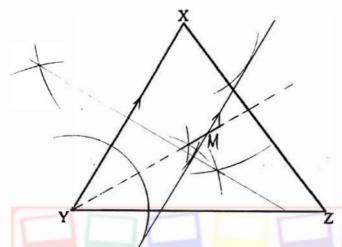
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(b) Determine the probability that the balls picked are of different colours. (2 marks)

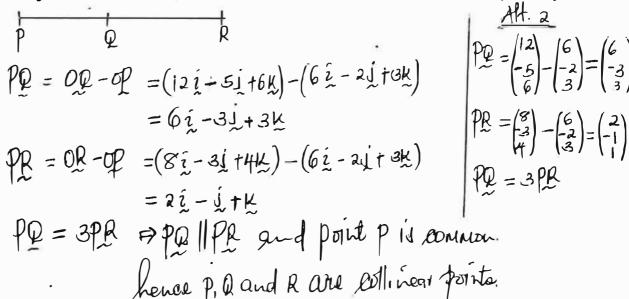


13. The figure below shows triangle XYZ.



Using a ruler and a pair of compasses, locate a point M on the triangle such that M is 2 cm from line YX and is equidistant from lines YX and YZ. Measure length YM. (3 marks)

14. The position vectors of points P, Q and R are OP = 6i - 2j + 3k, OQ = 12i - 5j + 6k and OR = 8i - 3j + 4k. Show that P, Q and R are collinear points. (3 marks)



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15. In a transformation an object of area x cm2 is mapped on to an image whose area is 13x cm2.

PDF Compressor Free Version Given that the matrix of the transformation is  $\begin{pmatrix} x & 7 \\ x-1 & 3x \end{pmatrix}$ , find the possible values of x. (3 marks)

ASF = 
$$\det f f \operatorname{maje} = A \cdot \operatorname{of} \operatorname{Image} A \cdot \operatorname{of} \operatorname{object}$$

$$\Rightarrow x(3x) - 7(x-1) = 13x = 13$$

$$\Rightarrow 3x^2 - 7x + 7 - 13 = 0$$

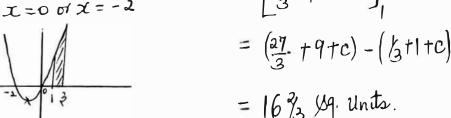
$$\Rightarrow 3x^2 - 9x + 2x - 6 = 0$$

$$\Rightarrow (x-3)(3x+2) = 0$$

$$\Rightarrow x-3 = 0 \text{ or } 3x+2 = 0 \Rightarrow x = 3 \text{ or } x = -\frac{7}{3}$$

16. Find the area enclosed by the curve  $y = x^2 + 2x$  the straight lines x = 1, x = 3 and the x-axis. (3 marks)

 $= \int_{0}^{3} (x^{2} + 2x) dx$ T.p at (-1,-1)  $= \left[\frac{\mathbf{I}^{3}}{3} + \chi^{2} + C\right]^{3}$ Z(X+2) = 0 T=0 of x=-2







## PDF Compressor Free FIGN II (50 marks)

Answer only five questions in this section in the spaces provided.

- 17. Pump P can fill an empty water tank in  $7\frac{1}{2}$  hours while pump Q can fill the same tank in  $11\frac{1}{4}$  hours. On a certain day, when the tank was empty, both pumps were opened for  $2\frac{1}{2}$  hours.
  - (a) Determine the fraction of the tank that was still empty at the end of the  $2\frac{1}{2}$  hours.

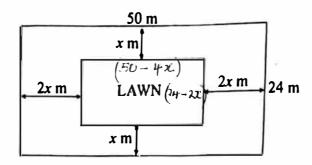
(b) Pump P was later opened alone to completely fill the tank. Determine the time it took pump P to fill the remaining fraction of the tank. (2 marks)

(c) The two pumps P and Q are operated by different proprietors. Water from the full tank was sold for Ksh 15 750. The money was shared between the two proprietors in the ratio of the quantity of water supplied by each.

Determine the amount of money received by the proprietor of pump P. (4 marks)



18. A rectangular plot measures 50 m by 24 m. A lawn, rectangular in shape, is situated inside the PDF plot with a same single shown in the figure below.



The width of the path in x m between the lengths of the lawn and those of the plot and 2x m between the widths of the lawn and those of the plot.

(a) Form and simplify an expression in x for the area of the:

(i) lawn;

(ii) path.

$$(50x24) - (8x^2 - 196x + 1200)$$



- (b) PDHe aremprinessan if the thressing area of the lawn.
  - (i) Form an equation in x and hence solve for x.

(4 marks)

$$-81^{2}+196x = 1.5(8x^{2}-196x+1200)$$

$$-20x^{2}+490x-180 = 0$$
of  $22^{2}-49x+180 = 0$ 

$$(2x-9)(x-20) = 0$$

$$2x-9 = 0 \text{ of } x-20 = 0$$

$$\Rightarrow x = 4/2 \text{ or } x = 20$$

(ii) Determine the perimeter of the lawn.

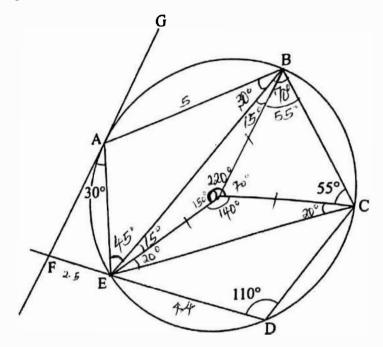
(3 marks)

appropriate value of 
$$x = 4\frac{1}{2}$$
  
Length of brun =  $50 - 4x + 6 = 32M$   
Width of lawn =  $24 - 2x + 6 = 15M$   
Persineter =  $2(32 + 15) = 94M$ 



19. In the figure below, points A, B, C, D and E lie on the circumference of a circle centre 0.

PDF Cinarpa Construction of the circle is produced to intersect with the tangent at F. Angle FAE = 30°, \( \neq EDC = 110° \) and \( \neq OCB = 55°.



(a) Determine the size of:

(i) 
$$\angle AEC. = 180^{\circ} - (70 + 30)^{\circ}$$

(3 marks

(ii) 
$$\angle AEB. = 80^{\circ} - (20 + 15)^{\circ}$$
  
= 4.5°

(3 marks

(b) Given that AB = 5 cm, ED = 4.4 cm and FE = 2.5 cm. Calculate correct to 1 decimal place:

(i) the radius of the circle.

(ii)

(2 mark

(2 mark

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## The table below shows income tax rates in a certain year. PDF Compressor Free tax rates in a certain year. 20.

Monthly taxable income in Kenya shillings	Tax rates
0 – 12 298	10%
12 299 – 23 885	15%
23 886 – 35 472	20%
35 473 – 47 059	25%
47 060 and above	30%

In the year, the monthly carnings of Kanini were as follows:

Basic salary

Ksh 64 500

House allowance

Ksh 12 000

Kanini contributes 7.5 % of her basic salary to a pension scheme. This contribution is exempted from taxation. She is entitled to a personal tax relief of Ksh 1 408 per month.

### Calculate:

(a) Kanini's monthly taxable income. (2 marks)

280

= Kuh 71662.50

$$= Ksh 7/662.50$$
the tax payable by Kanini that month.

| band :  $|0\% \times |2.298 = Ksh 1.229.80$ 

24 land :  $|5\% \times ||.587 = Ksh 1.738.05$ 

35 land :  $|25\% \times ||.587 = Ksh 2.317.40 +$ 

4th land :  $|25\% \times ||.587 = Ksh 2.896.75$ 

5th land :  $|30\% \times 24608.60 = Ksh 7.38|.05$ 

Grows fax =  $|Ksh ||.563.05$ 

\*(Not fax =  $|Ksh ||.563.05 - |Ksh ||.4156.05$ )

Examini's net pay that month.

Not fax =  $|Ksh ||.563.05$ 

(c)

Net tax = KSh 14 155.05 Pension =  $\frac{16h + 837.50}{164}$ Total deductions = KSh 18 992.55

Net pay = 76 500-18 992.55 = KCL 57 507.45

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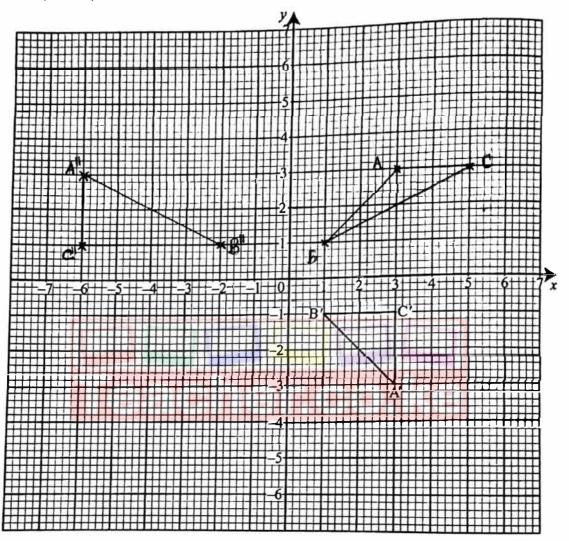




The vertices of the triangle shown on the grid are A'(3,-3), B'(1,-1) and C'(3,-1). 21.

**PDF Compressor Free Version** Triangle A'B'C' is the image of triangle ABC under a transformation whose matrix

is 
$$\begin{pmatrix} 0 & 1 \\ 1 & -2 \end{pmatrix}$$



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USIND INV. 
$$\Rightarrow$$

$$\begin{pmatrix}
2 & 1 & 3 & 6 & 0 \\
1 & 0 & 3 & -1 & -1
\end{pmatrix}$$
Scanned with CamScanner
$$\Rightarrow A(3,3), B(1,1), C(5,3)$$



(b) Triangle A"B"C" is the image of triangle A'B'C' under a transformation matrix PDF Compressor Free Version

$$\begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix}$$

(2 marks)

Determine the coordinates of A", B" and C".

$$\begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} 3 & 1 & 3 \\ -3 & -1 & -1 \end{pmatrix} = \begin{pmatrix} -6 & -2 & -6 \\ 3 & 1 & 1 \end{pmatrix}$$

(c) On the same grid provided, draw triangles ABC and A"B"C".

(2 marks)



(d) Determine a single matrix that maps ABC onto A"B"C".

(2 marks)

ABC 
$$\frac{NM}{(NM)^{-1}} A^{\parallel}B^{\parallel}C$$

$$|QL M = \begin{pmatrix} 0 & 1 \\ 1 & -2 \end{pmatrix}, N = \begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix}$$

$$NM = \begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & -2 \end{pmatrix} = \begin{pmatrix} 0 & -2 \\ -1 & 2 \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 0 & -2 \\ -1 & 2 \end{pmatrix}$$



# 22. Workers in a factory commute from their homes to the factory. The table below shows the PD distance restanting the workers.

Distance (km)	1 ~ 5	6 – 10	11 – 15	16 – 20	21 – 25	26 – 30
Number of workers	3	6	1	7	4	2

The mean distance covered was 14.5 km.

(a) Determine the value of t and hence the standard deviation of the distances correct to 2 decimal places. (6 marks

2	decimal p	laces.				(O IIIai K3)
Distance	<u> </u>	X	fx	d=X-14	.5 fa2	(i) $\frac{331+13t}{22+t} = 14.5$
1-5	3	3	a	-11.5	376,75	
6-10	6	8	48	-6.5	253.5	331 +13t=14.5(22+t)
11-15	1=3	13	13t	-1.5	8	t = 8
16-20	7	18	126	3.5	85.75	$(ii) S = \sqrt{\frac{2fd^2}{2f}}$
21 - 25	4	23	92	8.5	289	125
26-30	2	28	56	_13.5	364.5	= 1407.5
	22+t	Ш	331+1	3t	1407.5	30
	T.			101	60	= 6.85 KM

(b) Calculate, correct to 2 decimal places, the interquartile range of the distances. (4 marks)

Distance	_f	cf	<b>a</b>
15			41 — 年100 — 1.5
6-10	_		$=5.5 + \left(\frac{7.5 - 3}{6}\right) \times 5 = 9.25 \text{ KM}$
11-15	E	17	$Q_3 = 3/4 \times 30 = 22.5^{1/2}$
16-20	7	24	
21-25			= 15.5 + $\left(\frac{22.5-17}{7}\right)$ x5 = 19.43 Km
26-30	2 30	30	$Q_3 - Q_1 = 19.43 - 9.25 = 10.18 \text{ KM}$

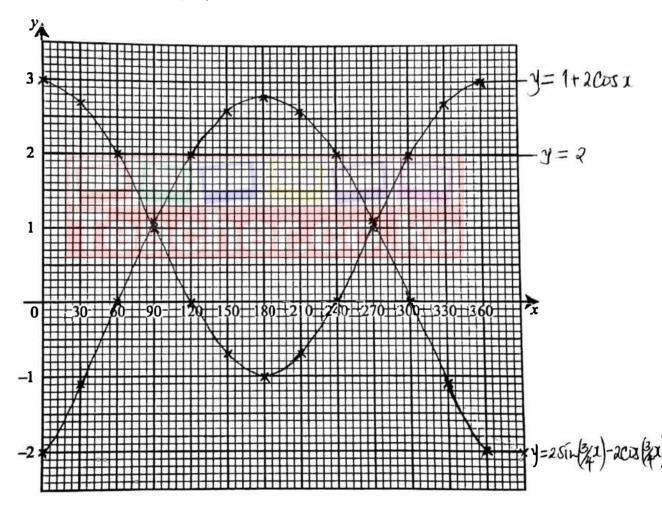


# 23. (a) Complete the table below giving the values correct to 1 decimal place.

PDF Compressor	Free	Vers	ion										
x°	0	30	60	90	120	150	180	210	240	270	300	330	360
$y = 2\sin\left(\frac{3}{4}x\right) - 2\cos\left(\frac{3}{4}x\right)$	-2	-1.1	0		2	2.6	2.8	2.6	) 2	1.1	0	<del>-1.1</del>	-2
$y=1+2\cos x$	3	2.7)	2	1	0	-0.7	-1 (	-0.7	0	1	(2)	2.7	3

(2 marks)

(b) On the grid provided and using the same axis, draw the graphs of 
$$y = 2\sin\left(\frac{3}{4}x\right) - 2\cos\left(\frac{3}{4}x\right)$$
 and  $y = 1 + 2\cos x$  for  $0^{\circ} \le x \le 360^{\circ}$ . (4 marks)





(2 marks)

(c) Using the graphs in part (b):

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(i) find the values of x for which  $\sin\left(\frac{3}{4}x\right) = 1 + \cos\left(\frac{3}{4}x\right)$ .  $y = 2 \left[Siu\left(\frac{3}{4}x\right) - Cot\left(\frac{3}{4}x\right)\right]$   $y = \left[Sii\left(\frac{3}{4}x\right) - Cot\left(\frac{3}{4}x\right)\right]$ 1 = [sin(3/1) - coo(3/2)] = 1

> $\Rightarrow x = 120^{5} \cdot 3240^{5}$ determine the range of x for which  $2\sin\left(\frac{3}{4}x\right) - 2\cos\left(\frac{3}{4}x\right) > 1 + 2\cos x$ . (ii)





- A particle was moving along a straight line. The acceleration of the particle after t seconds was Pribe to the particle was 18 ms<sup>-1</sup>.
  - (a) Determine the value of t when the particle is momentarily at rest.

(5 marks)

$$V = \int a dt$$

$$= \int (4t - 13) dt$$

$$= 2t^{2} - 13t + c$$
alt initial valueity,  $t = 0$ ,  $V = 18 \Rightarrow c = i8$ 

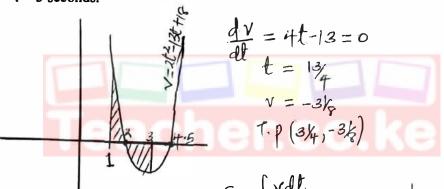
$$V = 2t^{2} - 13t + 18$$

$$But V = 0 = 2t^{2} - 13t + 18$$

$$\Rightarrow (t - 2)(2t - 9) = 0$$

$$t - 2 = 0 \text{ at } -9 = 0 \Rightarrow t = 2 \text{ sec. of } t = 4.5 \text{ sec.}$$

(b) Find the distance covered by the particle between the time t = 1 second and t = 3 seconds. (5 marks)



$$S = \int v dt$$

$$= \int_{3}^{2} (2t^{2} - 13t + 18) dt + \int_{3}^{3} (2t^{2} - 13t + 18) dt$$

$$= \left[ 3t^{3} - 13t^{2} + 18t + c \right]^{3} + \left[ 23t^{3} - 13t^{2} + 18t + c \right]^{3}$$

$$= 3\frac{1}{6} + \left[ -\frac{1}{6} \right]$$

$$= 3\frac{1}{6} + \frac{1}{6}$$

$$= 5 \text{ Matrics.}$$

### THIS IS THE LAST PRINTED PAGE.

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