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Markscheme

May 2019

Mathematics

Standard level

Paper 1



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Instruction De Examplessor Free Version

Abbreviations

- **M** Marks awarded for attempting to use a valid **Method**; working must be seen.
- (M) Marks awarded for a valid Method; may be implied by correct subsequent working.
- A Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- (A) Marks awarded for an **Answer** or for **Accuracy**; may be implied by **correct** subsequent working.
- **R** Marks awarded for clear **Reasoning**.
- **N** Marks awarded for **correct** answers if **no** working shown.
- **AG** Answer given in the question and so no marks are awarded.

Using the markscheme

1 General

Mark according to RM assessor instructions.

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award M0 followed by A1, as A mark(s) depend on the preceding M mark(s), if any. An exception to this rule is when work for M1 is missing, as opposed to incorrect (see point 4).
- Where *M* and *A* marks are noted on the same line, *eg M1A1*, this usually means *M1* for an **attempt** to use an appropriate method (*eg* substitution into a formula) and *A1* for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies (M2), N3, etc., do not split the marks, unless there is a note.
- Most **M** marks are for a **valid** method, ie a method which can lead to the answer: it must indicate some form of progress towards the answer.
- Once a correct answer to a question or part-question is seen, ignore further correct working. However, if further working indicates a lack of mathematical understanding do not award final *A1*.

3 N marks

If **no** working shown, award **N** marks for **correct** answers. In this case, ignore mark breakdown (**M**, **A**, **R**).

- Do not award a mixture of N and other marks.
- There may be fewer **N** marks available than the total of **M**, **A** and **R** marks; this is deliberate as it penalizes candidates for not following the instruction to show their working.
- There may not be a direct relationship between the *N* marks and the implied marks. There are times when all the marks are implied, but the *N* marks are not the full marks: this indicates that we want to see some of the working, without specifying what.

- For consistency within the marks liberne, **N** marks are noted for every part, even when these match the mark breakdown.
- If a candidate has incorrect working, which somehow results in a correct answer, do **not** award the **N** marks for this correct answer. However, if the candidate has indicated (usually by crossing out) that the working is to be ignored, award the **N** marks for the correct answer.

4 Implied and must be seen marks

Implied marks appear in brackets eg (M1).

- Implied marks can only be awarded if the work is seen or if implied in subsequent working (a correct final answer does not necessarily mean that the implied marks are all awarded). There are questions where some working is required, but as it is accepted that not everyone will write the same steps, all the marks are implied, but the *N* marks are not the full marks for the question.
- Normally the correct work is seen in the next line.
- Where there is an (*M1*) followed by *A1* for each correct answer, if no working shown, one correct answer is sufficient evidence to award the (*M1*).

Must be seen marks appear without brackets eg M1.

- Must be seen marks can only be awarded if the work is seen.
- If a must be seen mark is not awarded because work is missing (as opposed to M0 or A0 for incorrect work) all subsequent marks may be awarded if appropriate.

5 Follow through marks (only applied after an error is made)

Follow through (FT) marks are awarded where an incorrect answer (final or intermediate) from one part of a question is used correctly in subsequent part(s) or subpart(s). Usually, to award FT marks, there must be working present and not just a final answer based on an incorrect answer to a previous part. However, if the only marks awarded in a subpart are for the final answer, then FT marks should be awarded if appropriate. Examiners are expected to check student work in order to award FT marks where appropriate.

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** and **R** marks may be awarded if appropriate. (However, as noted above, if an **A** mark is not awarded because work is missing, all subsequent marks may be awarded if appropriate).
- Exceptions to this rule will be explicitly noted on the markscheme.
- If the question becomes much simpler because of an error then use discretion to award fewer **FT** marks.
- If the error leads to an inappropriate value (*eg* probability greater than 1, use of r > 1 for the sum of an infinite GP, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word "**their**" in a description, to indicate that candidates may be using an incorrect value.
- If a candidate makes an error in one part, but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the question says hence. It is often possible to use a different approach in subsequent parts that does not depend on the answer to previous parts.
- In a "show that" question, if an error in a previous subpart leads to not showing the required answer, do not award the final **A1**. Note that if the error occurs within the same subpart, the **FT** rules may result in further loss of marks.

6 MisPleEdCompressor Free Version

If a candidate incorrectly copies information from the question, this is a mis-read (**MR**). A candidate should be penalized only once for a particular mis-read. Use the **MR** stamp to indicate that this is a misread. Do not award the first mark in the question, even if this is an **M** mark, but award all others (if appropriate) so that the candidate only loses one mark for the misread.

- If the question becomes much simpler because of the MR, then use discretion to award fewer marks.
- If the MR leads to an inappropriate value (eg probability greater than 1, use of r > 1 for the sum of an infinite GP, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.

7 Discretionary marks (d)

An examiner uses discretion to award a mark on the rare occasions when the markscheme does not cover the work seen. In such cases the annotation DM should be used and a brief **note** written next to the mark explaining this decision.

8 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If in doubt, contact your team leader for advice.

- Alternative methods for complete parts are indicated by METHOD 1, METHOD 2, etc.
- Alternative solutions for parts of questions are indicated by **EITHER** . . . **OR**. Where possible, alignment will also be used to assist examiners in identifying where these alternatives start and finish.

9 Alternative forms

Unless the question specifies otherwise, accept equivalent forms.

- As this is an international examination, accept all alternative forms of **notation**.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, **simplified** answers, (which candidates often do not write in examinations), will generally appear in brackets. Marks should be awarded for either the form preceding the bracket or the form in brackets (if it is seen).

10 Calculators

No calculator is allowed. The use of any calculator on paper 1 is malpractice, and will result in no grade awarded. If you see work that suggests a candidate has used any calculator, please follow the procedures for malpractice. Examples: finding an angle, given a trig ratio of 0.4235.

11 Style

The markscheme aims to present answers using good communication, eg if the question asks to find the value of k, the markscheme will say k=3, but the marks will be for the correct value 3- there is usually no need for the "k=". In these cases, it is also usually acceptable to have another variable, as long as there is no ambiguity in the question, eg if the question asks to find the value of p and of p, then the student answer needs to be clear. Generally, the only situation

where the full answers required in this case the markscheme will say "must be an equation".

The markscheme often uses words to describe what the marks are for, followed by examples, using the eg notation. These examples are not exhaustive, and examiners should check what candidates have written, to see if they satisfy the description. Where these marks are **M** marks, the examples may include ones using poor notation, to indicate what is acceptable.

12 Candidate work

If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work.

Candidates are meant to write their answers to Section A on the question paper (QP), and Section B on answer booklets. Sometimes, they need more room for Section A, and use the booklet (and often comment to this effect on the QP), or write outside the box. That is fine, and this work should be marked.

The instructions tell candidates not to write on Section B of the QP. Thus they may well have done some rough work here which they assume will be ignored. If they have solutions on the answer booklets, there is no need to look at the QP. However, if there are whole questions or whole part solutions missing on answer booklets, please check to make sure that they are not on the QP, and if they are, mark those whole questions or whole part solutions that have not been written on answer booklets.

13. Diagrams

The notes on how to allocate marks for sketches usually refer to passing through particular points or having certain features. These marks can only be awarded if the sketch is approximately the correct shape. All values given will be an approximate guide to where these points/features occur. In some questions, the first A1 is for the shape, in others, the marks are only for the points and/or features. In both cases, unless the shape is approximately correct, no marks can be awarded (unless otherwise stated). However, if the graph is based on previous calculations, FT marks should be awarded if appropriate.

14. Accuracy of Answers

If the level of accuracy is specified in the question, a mark will be allocated for giving the final answer to the required accuracy. When this is not specified in the question, all numerical answers should be given exactly or correct to three significant figures.

Do not accept unfinished numerical final answers such as 3/0.1 (unless otherwise stated). As a rule, numerical answers with more than one part (such as fractions) should be given using integers (eg 6/8). Calculations which lead to integers should be completed, with the exception of fractions which are not whole numbers. Intermediate values do not need to be given to the correct three significant figures. But, if candidates work with rounded values, this could lead to an incorrect answer, in which case award A0 for the final answer.

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1. (a) valid approach

(M1)

eg
$$0.3-0.1$$
, $p+0.1=0.3$

$$p = 0.2$$

A1

[2 marks]

(b) valid approach

(M1)

eg
$$1-(0.3+0.4)$$
, $1-0.4-0.1-p$

$$q = 0.3$$

A1

N2

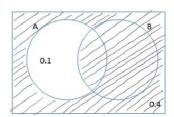
[2 marks]

N2

(c) valid approach

(M1)

eg
$$0.7+0.5-0.3$$
, $p+q+0.4$, $1-0.1$, $P(A' \cup B) = P(A') + P(B) - P(A' \cap B)$,



$$P(A' \cup B) = 0.9$$

A1

N2

[2 marks]

Total [6 marks]

$$eg -3+6s=15, 6s=18$$

$$s=3 (A1)$$

substitute their s value into z component (M1)

eg
$$10+3(2)$$
, $10+6$

$$c=16$$

[4 marks]

N3

(b)
$$r = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} + t \begin{pmatrix} 6 \\ 0 \\ 2 \end{pmatrix} \left(= \left(\mathbf{i} + 2\mathbf{j} + 3\mathbf{k} \right) + t \left(6\mathbf{i} + 2\mathbf{k} \right) \right)$$
 A2 N2

Note: Accept any scalar multiple of $\begin{pmatrix} 6 \\ 0 \\ 2 \end{pmatrix}$ for the direction vector.

Award
$$\mathbf{A1}$$
 for $\begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} + t \begin{pmatrix} 6 \\ 0 \\ 2 \end{pmatrix}$, $\mathbf{A1}$ for $L_2 = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} + t \begin{pmatrix} 6 \\ 0 \\ 2 \end{pmatrix}$, $\mathbf{A0}$ for $r = \begin{pmatrix} 6 \\ 0 \\ 2 \end{pmatrix} + t \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$.

[2 marks]

Total [6 marks]

3. (a) Philagomagessor Free Version

(M1)

eg labelled sides on separate triangle, $\sin^2 x + \cos^2 x = 1$

correct working

(A1)

eg missing side is 4, $\sqrt{1-\left(\frac{3}{5}\right)^2}$

 $\cos\theta = \frac{4}{5}$

A1

N3

[3 marks]

(b) correct substitution into $\cos 2\theta$

(A1)

eg
$$2\left(\frac{16}{25}\right) - 1$$
, $1 - 2\left(\frac{3}{5}\right)^2$, $\frac{16}{25} - \frac{9}{25}$

 $\cos 2\theta = \frac{7}{25}$

A1

N2

[2 marks]

(c) correct working

(A1)

eg
$$\frac{7}{25} = \frac{14}{BC}$$
, $BC = \frac{14 \times 25}{7}$

BC = 50 (cm)

A1

N2

[2 marks]

Total [7 marks]

4. (a) PRE Compressor EggstiVersion

A1 N1 [1 mark]

(b) interchanging x and y (seen anywhere) (M1)

eg
$$x = \frac{2y-1}{y+3}$$
, $x(y+3) = 2y-1$

evidence of correct manipulation

(A1)

eg
$$yx+3x=2y-1$$
, $y(x-2)=-3x-1$, $2-\frac{7}{y+3}$

$$f^{-1}(x) = \frac{-3x-1}{x-2} \left(= \frac{3x+1}{2-x}, \frac{7}{2-x} - 3 \right) \text{ (accept } y = 1)$$

[3 marks]

(c) valid approach to find horizontal asymptote (M1)

eg
$$\frac{-3}{1}$$
, vert.asymp of f becomes horiz.asymp of f^{-1} , $\frac{-3(x-2)+5}{x-2}$, $x \to \infty$

$$y = -3$$
 (must be an equation)

A1

[2 marks]

N2

Total [6 marks]

eg
$$\int f'$$
, $\int 2e^{-3x} dx$, $du = -3$

correct integral (do not penalize for missing
$$+C$$
) (A2)

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$$eg \qquad -\frac{2}{3}e^{-3x} + C$$

substituting $\left(\frac{1}{3},5\right)$ (in any order) into **their** integrated expression (must have +C) **M1**

eg
$$-\frac{2}{3}e^{-3(1/3)} + C = 5$$

Note: Award *M0* if they substitute into original or differentiated function.

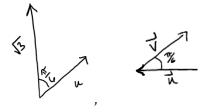
$$f(x) = -\frac{2}{3}e^{-3x} + 5 + \frac{2}{3}e^{-1} \text{ (or any equivalent form, eg } -\frac{2}{3}e^{-3x} + 5 - \frac{2}{-3e})$$

[5 marks]

6. METHOD COUNTRESSON Free Version

diagram including u, v and included angle of $\frac{\pi}{6}$ (M1)

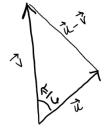
eg

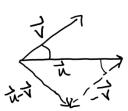


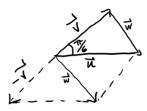
sketch of triangle with w (does not need to be to scale)

(A1)

eg







choosing cosine rule

$$eg \qquad a^2 + b^2 - 2ab\cos C$$

A1

(A1)

(M1)

correct substitution

eg $4^2 + (\sqrt{3})^2 - 2(4)(\sqrt{3})\cos\frac{\pi}{6}$

$$\cos\frac{\pi}{6} = \frac{\sqrt{3}}{2}$$
 (seen anywhere) (A1)

correct working

eg
$$16+3-12$$

$$|w| = \sqrt{7}$$
 A1 N2

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METHOD 2 (scalar product)

eg
$$|\mathbf{w}|^2 = (\mathbf{u} - \mathbf{v}) \cdot (\mathbf{u} - \mathbf{v}), |\mathbf{w}|^2 = \mathbf{u} \cdot \mathbf{u} - 2\mathbf{u} \cdot \mathbf{v} + \mathbf{v} \cdot \mathbf{v}, |\mathbf{w}|^2 = (u_1 - v_1)^2 + (u_2 - v_2)^2,$$

 $|\mathbf{w}| = \sqrt{(u_1 - v_1)^2 + (u_2 - v_2)^2 + (u_3 - v_3)^2}$

correct value for
$$u \cdot u$$
 (seen anywhere) (A1)

eg
$$|\mathbf{u}|^2 = 16$$
, $\mathbf{u} \cdot \mathbf{u} = 16$, $u_1^2 + u_2^2 = 16$

correct value for
$$v \cdot v$$
 (seen anywhere) (A1)

eg
$$|\mathbf{v}|^2 = 3$$
, $\mathbf{v} \cdot \mathbf{v} = 3$, $v_1^2 + v_2^2 + v_3^2 = 3$

$$\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$$
 (seen anywhere)

$$u \cdot v = 4 \times \sqrt{3} \times \frac{\sqrt{3}}{2}$$
 (= 6) (seen anywhere)

correct substitution into $u \cdot u - 2u \cdot v + v \cdot v$ or $u_1^2 + u_2^2 + v_1^2 + v_2^2 - 2(u_1v_1 + u_2v_2)$ (2 or 3 dimensions) (A1)

eg
$$16-2(6)+3 = 7$$

$$|w| = \sqrt{7}$$
A1 N2
[7 marks]

(M1)

eg
$$\int v = s$$
, $s' = v$

$$s(4) - s(2) = 9$$

A1

N2 [2 marks]

(b) correctly interpreting distance travelled in first 2 seconds (seen anywhere, including part (a) or the area of 15 indicated on diagram) (A1)

– 14 –

eg
$$\int_0^2 v = 15$$
, $s(2) = 15$

valid approach to find total distance travelled

(M1)

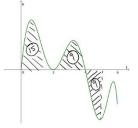
eg sum of 3 areas, $\int_0^4 v + \int_4^5 v$, shaded areas in diagram between 0 and 5

Note: Award **M0** if only $\int_0^5 |v|$ is seen.

correct working towards finding distance travelled between 2 and 5 (seen anywhere including within total area expression or on diagram) (A1)

eg
$$\int_{2}^{4} v - \int_{4}^{5} v$$
, $\int_{2}^{4} v = \int_{4}^{5} |v|$, $\int_{4}^{5} v \, dt = -9$, $s(4) - s(2) - [s(5) - s(4)]$,

equal areas



correct working using s(5) = s(2)

(A1)

eg
$$15+9-(-9)$$
, $15+2[s(4)-s(2)]$, $15+2(9)$, $2\times s(4)-s(2)$, $48-15$

total distance travelled = 33 (m)

A1

[5 marks]

N₂

Total [7 marks]

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8. (a) valid approach (M1)

eg f(x) = 0, $9 - x^2 = 0$, one correct solution

x = -3, 3 (accept (3, 0), (-3, 0))

A1 N2 [2 marks]

(b) valid approach (M1)

eg height = f(b), base = 2(OP) or 2b, $2b(9-x^2)$, $2b \times f(b)$

correct working that clearly leads to given answer A1

eg $2b(9-b^2)$

Note: Do not accept sloppy notation eg $2b \times 9 - b^2$.

area = $18b - 2b^3$ AG N0 [2 marks]

(c) setting derivative = 0 (seen anywhere) (M1)

eg A' = 0, $[18b - 2b^3]' = 0$

correct derivative (must be in terms of b only) (seen anywhere) A2

eg $18-6b^2$, $2b(-2b)+(9-b^2)\times 2$

correct working (A1)

eg $6b^2 = 18$, $b = \pm \sqrt{3}$

 $b=\sqrt{3}$ A1 N3 [5 marks]

(d) valid approach (M1)

eg f = g, $9-x^2 = (x-3)^2 + k$

correct working (A1)

eq $9-x^2=x^2-6x+9+k$. $9-x^2-x^2+6x-9-k=0$

 $2x^{2}-6x+k=0$ AG N0

[2 marks]

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(e) METHOD 1 (discriminant)

recognizing to use discriminant (seen anywhere) (M1)

eg Δ , $b^2 - 4ac$

discriminant = 0 (seen anywhere)

correct substitution into discriminant (do not accept only in quadratic formula) (A1)

eg $(-6)^2 - 4(2)(k)$, $(6)^2 - 4(2)(k)$

correct working (A1)

eg 36-8k=0, 8k=36

$$k = \frac{36}{8} \left(= \frac{9}{2}, \ 4.5 \right)$$
 A1 N2

METHOD 2 (completing the square)

valid approach to complete the square (M1)

eg $2\left(x^2 - 3x + \frac{9}{4}\right) = -k + \frac{18}{4}$, $x^2 - 3x + \frac{9}{4} - \frac{9}{4} + \frac{k}{2} = 0$

correct working (A1)

eg $2\left(x-\frac{3}{2}\right)^2 = -k + \frac{18}{4}, \left(x-\frac{3}{2}\right)^2 - \frac{9}{4} + \frac{k}{2} = 0$

recognizing condition for one solution M1

eg $\left(x-\frac{3}{2}\right)^2=0, -\frac{9}{4}+\frac{k}{2}=0$

correct working (A1)

 $eg -k = -\frac{18}{4}, \frac{k}{2} = \frac{9}{4}$

$$k = \frac{18}{4} \left(= \frac{9}{2}, \ 4.5 \right)$$
 A1 N2

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METHOD 3 (using vertex)

valid approach to find vertex (seen anywhere) M1

eg
$$(2x^2 - 6x + k)' = 0, -\frac{b}{2a}$$

correct working (A1)

eg
$$(2x^2-6x+k)'=4x-6, -\frac{(-6)}{2(2)}$$

$$x = \frac{6}{4} \left(= \frac{3}{2} \right) \tag{A1}$$

correct substitution (A1)

eg
$$2\left(\frac{3}{2}\right)^2 - 6\left(\frac{3}{2}\right) + k = 0$$

$$k = \frac{18}{4} \left(= \frac{9}{2}, \ 4.5 \right)$$
 A1 N2

[5 marks]

Total [16 marks]

(M1)

eg
$$a+x+b=1$$
, $100-a-b$, $1-a+b$

A1

$$P(-1.6 < z < 2.4) = 1 - a - b \ (= 1 - (a + b))$$

[2 marks]

N₂

(b)
$$P(z > -1.6) = 1 - a$$
 (seen anywhere)

(A1)

(M1)

eg
$$P(A|B)$$
, $P(B|A)$

correct working

(A1)

eg
$$\frac{P(z < 2.4 \cap z > -1.6)}{P(z > -1.6)}, \frac{P(-1.6 < z < 2.4)}{P(z > -1.6)}$$

$$P(z < 2.4 | z > -1.6) = \frac{1-a-b}{1-a}$$

N4

Note: Do not award the final A1 if correct answer is seen followed by incorrect simplification.

[4 marks]

(c)
$$z = -1.6$$
 (may be seen in part (d))

A1

A1

N1

Note: Depending on the candidate's interpretation of the question, they may give $\frac{1-m}{s}$ as the answer to part (c). Such answers should be awarded the first **(M1)** in part (d), even when part (d) is left blank. If the candidate goes on to show z = -1.6 as part of their working in part (d), the **A1** in part (c) may be awarded.

[1 mark]

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(d) attempt to standardize
$$x$$
 (do not accept $\frac{x-\mu}{\sigma}$) (M1)

eg
$$\frac{1-m}{s}$$
 (may be seen in part (c)), $\frac{m-2}{s}$, $\frac{x-m}{\sigma}$

correct equation with each z-value (A1)(A1)

eg
$$-1.6 = \frac{1-m}{s}$$
, $2.4 = \frac{2-m}{s}$, $m+2.4s=2$

valid approach (to set up equation in one variable)

eg
$$2.4 = \frac{2 - (1.6s + 1)}{s}, \frac{1 - m}{-1.6} = \frac{2 - m}{2.4}$$

correct working (A1)

eg
$$1.6s+1=2-2.4s$$
, $4s=1$, $m=\frac{7}{5}$

$$s = \frac{1}{4}$$
 A1 N2

[6 marks]

Total [13 marks]

(A1)

(A1)

eg $\sin\left(\frac{\pi}{4}x\right) = 1$, $\sqrt{x}\left(1 - \sin\left(\frac{\pi}{4}x\right)\right) = 0$

$$\sin\left(\frac{\pi}{2}\right) = 1$$
 (seen anywhere) (A1)

correct working (ignore additional values)

eg
$$\frac{\pi}{4}x = \frac{\pi}{2}, \frac{\pi}{4}x = \frac{\pi}{2} + 2\pi$$

x = 2, 10 A1A1 N1N1 [5 marks]

(b) correct working (A1)

eg d=10-2, a+b=2, a+2b=10

valid approach (M1)

eg 2+(n-1)8, a+2(2-a)=10, b = common difference

a = -6, b = 8 (accept -6 + 8n) A1A1 N2N2 [4 marks]

(c) valid approach (M1)

eg first intersection at x = 0, n = 20

correct working A1

eg $-6+8\times20$, $2+(20-1)\times8$, $u_{20}=154$

 $P(154, \sqrt{154})$ (accept x = 154 and $y = \sqrt{154}$) **A1A1** N3

[4 marks]

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(d) valid attempt to find upper boundary (M1)

eg half way between
$$u_{20}$$
 and u_{21} , $u_{20}+\frac{d}{2}$, $154+4$, $-2+8n$, at least two values of new sequence $\{6,14,\ldots\}$

upper boundary at
$$x = 158$$
 (seen anywhere) (A1)

correct integral expression (accept missing dx)

eg
$$\int_0^{158} \left(\sqrt{x} \sin\left(\frac{\pi}{4}x\right) + \sqrt{x} \right) dx$$
, $\int_0^{158} \left(g + f\right) dx$), $\int_0^{158} \sqrt{x} \sin\left(\frac{\pi}{4}x\right) dx - \int_0^{158} -\sqrt{x} dx$

Note: Award *A1* for two correct limits and *A1* for correct integrand. The *A1* for correct integrand may be awarded independently of all the other marks.

[4 marks]

Total [17 marks]